

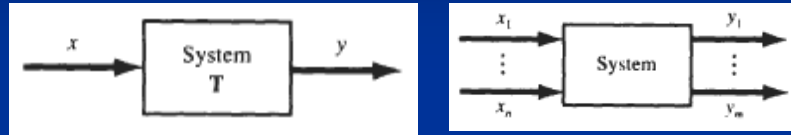
Sistem

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System

- System adalah
 - Interkoneksi dari komponen-komponen dengan terminal-terminal (masukan dan keluaran) materi, energi, atau informasi yang di dalamnya terdapat proses-proses tertentu
- Contoh system
 - Rangkaian elektronika
 - Robot
 - Pabrik/Industri
 - dll

single or multiple



- System with single or multiple input and output signals.

Continuous and Discrete Systems

- If the input and output signals x and y are continuous-time signals, then the system is called a ***continuous-time system***
- If the input and output signals are discrete-time signals or sequences, then the system is called a ***discrete-time system***



Systems with Memory and without Memory

- A system is said to be **memory-less** if the output at any time depends on only the input at that same time.
- Otherwise, the system is said to have **memory**. An example of a memoryless system is a resistor R

$$y(t) = Rx(t)$$

- An example of a system with memory is a capacitor

$$y(t) = \frac{1}{C} \int_{-\infty}^t x(\tau) d\tau$$

Causal and Non-causal Systems

- A system is called **causal** if its output $y(t)$ at an arbitrary time $t = t_0$ depends on only the input $x(t)$ for $t \leq t_0$. That is, the output of a causal system at the present time depends on only the present and/or past values of the input, not on its future values.
- A system is called **noncausal** if it is not causal. Examples of noncausal systems are

$$y(t) = x(t + 1)$$

$$y[n] = x[-n]$$

all memory-less systems are causal, but not vice versa.

Linear and Nonlinear Systems

- If the operator T satisfies the following two conditions, then T is called a linear operator and the system represented by a linear operator T is called a linear system:

- **Additivity**, Given that $T x_1 = y_1$ and $T x_2 = y_2$

$$T(x_1 + x_2) = T x_1 + T x_2 = y_1 + y_2$$

- **Scaling**, for any signals x and any scalar a .

$$T\{ax\} = a T x = ay$$

Time-Invariant and Time-Varying Systems

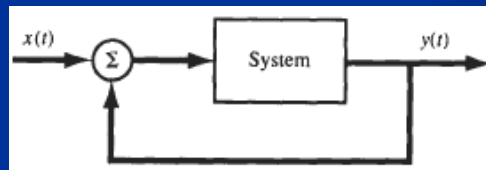
- A system is called time-invariant if a time shift (delay or advance) in the input signal causes the same time shift in the output signal.
- Thus, for a continuous-time system, the system is time-invariant if

$$T\{x(t - \tau)\} = y(t - \tau)$$

Linear Time-Invariant Systems. If the system is linear and also time-invariant, then it is called a linear time-invariant (LTI) system.

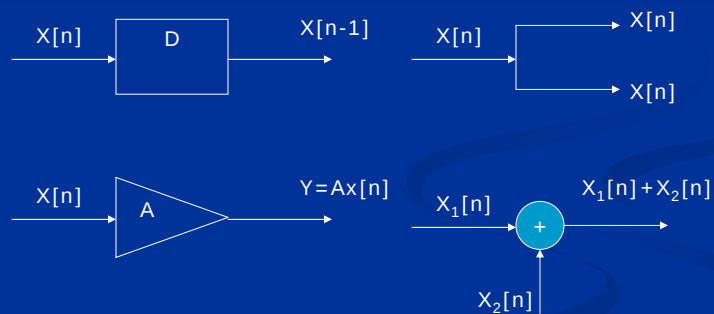
Feedback Systems

- A special class of systems of great importance consists of systems having **feedback**.
- In a **feedback system**, the output signal is fed back and added to the input to the system



Penggambaran Sistem

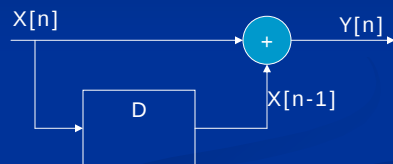
- Penggambaran sistem



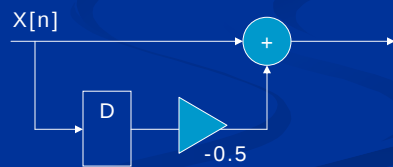
Penggambaran Sistem

■ Contoh

$$y[n] = x[n] + x[n-1]$$



$$y[n] = x[n] - 0.5x[n-1]$$



Penggambaran Sistem

■ Integral

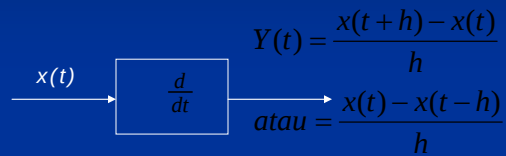


- Diskret Integral / Summation

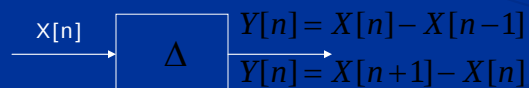


Penggambaran Sistem

■ Differential



- Differential diskret / Differences

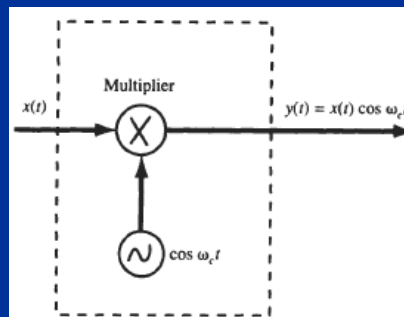


Example

- Consider the system shown in Figure. Determine whether it is

- (a) memoryless,
- (b) causal,
- (c) linear,
- (d) time-invariant, or
- (e) stable.

$$y(t) = \mathbf{T}\{x(t)\} = x(t) \cos \omega_c t$$



Example

- (a) Since the value of the output $y(t)$ depends on only the **present values** of the input $x(t)$, the system is memoryless.
- (b) Since the output $y(t)$ does not depend on the future values of the input $x(t)$, the system is causal.
- (c) Let $x(t) = a_1 x_1(t) + a_2 x_2(t)$. Then

$$\begin{aligned}
 y(t) &= T\{x(t)\} = [a_1 x_1(t) + a_2 x_2(t)] \cos \omega t \\
 &= a_1 x_1(t) \cos \omega t + a_2 x_2(t) \cos \omega t \\
 &= a_1 y_1(t) + a_2 y_2(t)
 \end{aligned}$$
 Thus, the superposition property is satisfied and the system is linear.

Example

- (d) Let $y_1(t)$ be the output produced by the shifted input $x_1(t) = x(t - t_0)$. Then

$$y_1(t) = T\{x(t - t_0)\} = x(t - t_0) \cos \omega t$$
 But

$$y(t - t_0) = x(t - t_0) \cos \omega_c(t - t_0) \neq y_1(t)$$
 Hence, the system is not time-invariant.
- (e) Since $\cos \omega_c t \leq 1$, we have

$$|y(t)| = |x(t) \cos \omega_c t| \leq |x(t)|$$
- Thus, if the input $x(t)$ is bounded, then the output $y(t)$ is also bounded and the system is stable.